

Sunday, April 07, 2019  
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**KEY**

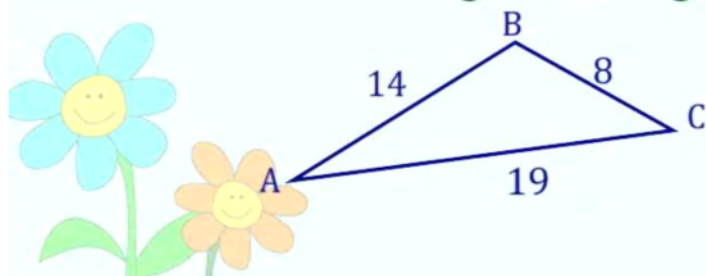
## 6.2 B Law of Cosines

Homework: • pg 443 #1,7,23,25  
• Quiz 6.1-6.2 -

Objective: • Optional 6.1VC and 6.2VC

SWBAT: Use the Law of Cosines to solve oblique triangles (SSS & SAS)

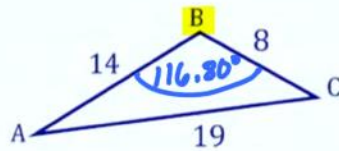
Do Now: Can we apply the Law of Sines to the given triangle?



*NO*

Example 1: Solve  $\triangle ABC$  (round to 2 decimal places)

SSS



**Important Note:**

When given SSS triangle, solve for the **★ largest angle FIRST ★** using the **Law of Cosines!!** Then use **Law of Sines** to find the other two acute angles.

$$\cos B = \frac{a^2 + c^2 - b^2}{2ac}$$

$$\cos B = \frac{(8)^2 + (14)^2 - (19)^2}{2(8)(14)}$$

$$\cos^{-1}(-.45089) = B$$

$$B \approx 116.80^\circ$$

$$\frac{a}{\sin A} = \frac{b}{\sin B}$$

$$\frac{8}{\sin A} = \frac{19}{\sin 116.8^\circ}$$

$$\sin A = \frac{8 \sin 116.8^\circ}{19}$$

$$\sin^{-1}(.3758) = A$$

$$A \approx 22.08^\circ$$

$$C = 180^\circ - A - B$$

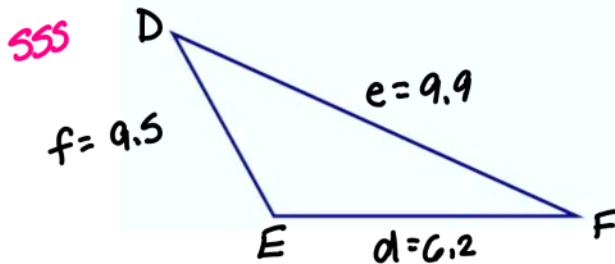
$$C = 180^\circ - 22.08^\circ - 116.8^\circ$$

$$C \approx 41.12^\circ$$

Hints:

- 1.) Don't forget to use **parentheses!**
- 2.) **Store** values that you will later use for another calculation!!

Example 2: Solve  $\triangle DEF$  given  $d = 6.2, e = 9.9, f = 9.5$



\* USE LAW of cosines to find largest  $\angle$

$$\cos E = \frac{d^2 + f^2 - e^2}{2df}$$

$$\cos E = \frac{(6.2)^2 + (9.5)^2 - (9.9)^2}{2(6.2)(9.5)} \leftarrow \text{STO}$$

$$\cos^{-1}(.26044) = E \leftarrow \text{STO}$$

$$E \approx 74.90^\circ$$

$$\frac{d}{\sin D} = \frac{e}{\sin E}$$

$$\frac{6.2}{\sin D} = \frac{9.9}{\sin 74.90^\circ}$$

$$\sin D = \frac{6.2 \sin 74.90^\circ}{9.9} \leftarrow \text{STO}$$

$$\sin^{-1}(.6046) = D \leftarrow \text{STO}$$

$$D \approx 37.20^\circ$$

$$F = 180^\circ - E - D$$

$$F \approx 180^\circ - 74.9^\circ - 37.20^\circ$$

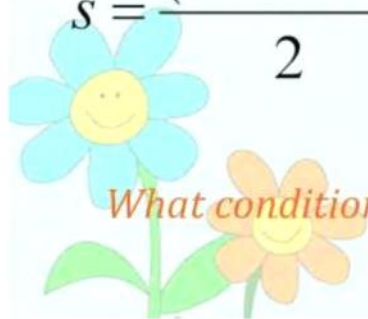
$$F \approx 67.89^\circ$$

## Heron's Area Formula

If  $ABC$  is a triangle with sides  $a$ ,  $b$ , and  $c$ , then:

$$\text{Area} = \sqrt{s(s-a)(s-b)(s-c)} \quad \text{where}$$

$$s = \frac{(a+b+c)}{2} \quad (s \text{ is the semi-perimeter})$$



*What condition must exist to use Heron's Formula?*

**SSS**

Use **Heron's Area Formula** to find the area of the triangle given:

$$\text{Area} = \sqrt{s(s-a)(s-b)(s-c)}$$
$$s = \frac{(a+b+c)}{2}$$

1.)  $a = 12, b = 15, c = 9$

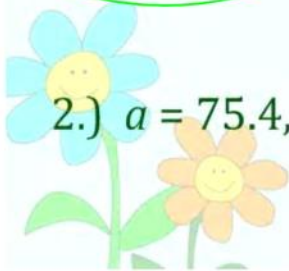
$$s = \frac{12+15+9}{2}$$

$$s = 18$$

$$A = \sqrt{18(18-12)(18-15)(18-9)}$$

$$A = \sqrt{2916}$$

$$A = 54 \text{ sq units}$$



2.)  $a = 75.4, b = 52, c = 52$

$$s = \frac{75.4 + 52 + 52}{2}$$

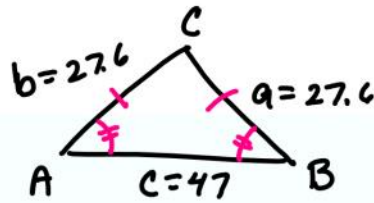
$$s = 89.7$$

$$A = \sqrt{89.7(89.7-75.4)(89.7-52)(89.7-52)}$$

$$A = \sqrt{1,823,102.896} \leftarrow 570$$

$$A \approx 1350.2 \text{ sq units}$$

## Your turn...



SSS

\* Solve for largest  $\angle$  1st!

1.) Solve  $\triangle ABC$  given  $a = 27.6$ ,  $b = 27.6$ ,  $c = 47$

$$\cos C = \frac{a^2 + b^2 - c^2}{2ab}$$

$$\cos C = \frac{(27.6)^2 + (27.6)^2 - 47^2}{2(27.6)(27.6)}$$

$$\cos^{-1}(-.44993) = C$$

$$C \approx 116.74^\circ$$

$$\frac{a}{\sin A} = \frac{c}{\sin C}$$

$$\frac{27.6}{\sin A} = \frac{47}{\sin 116.74^\circ}$$

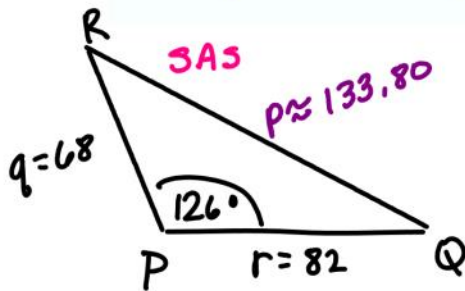
$$\sin A = \frac{27.6 \sin 116.74^\circ}{47}$$

$$A \approx 31.63^\circ$$

$$B \approx 31.63^\circ$$

A=B  
because  
Sides are  
equal

2.) Solve  $\triangle PQR$  given  $P = 126^\circ$ ,  $q = 68$ ,  $r = 82$



$$p^2 = q^2 + r^2 - 2qr \cos P$$

$$p^2 = (68)^2 + (82)^2 - 2(68)(82) \cos 126^\circ$$

$$p^2 = 17902.98113 \leftarrow \text{STO}$$

$$p \approx 133.80$$

$$\cos R = \frac{p^2 + q^2 - r^2}{2pq}$$

$$\cos R = \frac{(133.8)^2 + (68)^2 - (82)^2}{2(133.8)(68)}$$

$$\cos^{-1}(.8684186) = R$$

$$R \approx 29.72^\circ$$

$$Q = 180^\circ - P - R$$

$$Q = 180^\circ - 126^\circ - 29.72^\circ$$

$$Q \approx 24.28^\circ$$

OR

\* Use Law of Sines, since given an obtuse  $\angle$

$$\frac{p}{\sin P} = \frac{q}{\sin Q}$$

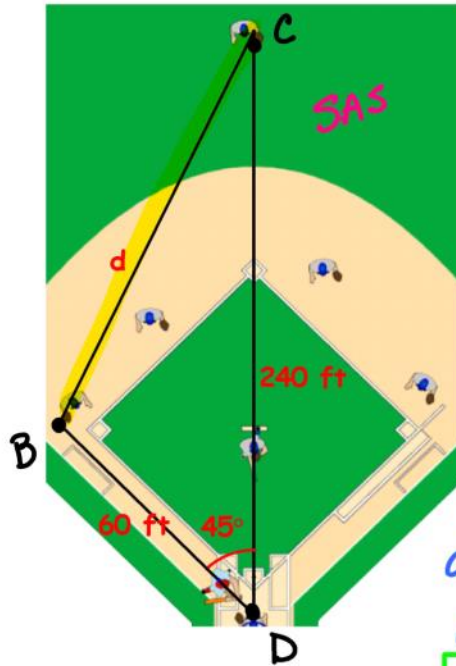
$$\frac{133.80}{\sin 126^\circ} = \frac{68}{\sin Q}$$

$$\sin Q = \frac{68 \sin 126^\circ}{133.8}$$

$$Q \approx 24.28^\circ$$



## Applications:



A centerfielder in a softball game fields the ball and throws to third plate. If the distance from the centerfielder to home plate is 240 feet and the distance between bases is 60 feet, how far did the centerfielder throw the ball?

$$d^2 = b^2 + c^2 - 2bc \cos D$$

$$d^2 = (240)^2 + (60)^2 - 2(240)(60) \cos 45^\circ$$

$$d^2 = 40835.3247$$

$$d \approx 202 \text{ feet}$$



## Summary:

- Law of Sines only works with AAS, ASA, SSA.
- Law of Cosines works with SSS, SAS
- Law of Cosines:  $c^2 = a^2 + b^2 - 2ab \cos C$

the first part is the Pythagorean Thm; then  
 $2*ab[\cos]c$

- Only one formula needed - **MEMORIZE**. Plug all info into this, then solve for angle.
- The Law of Cosines is a form of Pythagorean Thm
- YOU DO NOT KNOW IF YOU HAVE AN OBTUSE ANGLE USING SINE.
- Only one obtuse angle in  $\Delta$ , so find largest angle first then use Law of Sines or Law of Cosines to find remaining (acute) angles. Law of Sines is easier to use, but dependent upon previously found values (therefore **MAY** be incorrect)
- When using **Law of COSINES**, find **LARGEST ANGLE FIRST!!!** If you use the **Law of SINES**, find the **SMALLEST ANGLES FIRST!!!**