5.4 In Exercises 51–54, find the exact values of the sine, cosine, and tangent of the angle by using a sum or difference formula.

51.
$$285^{\circ} = 315^{\circ} - 30^{\circ}$$

52.
$$345^{\circ} = 300^{\circ} + 45^{\circ}$$

53.
$$\frac{25\pi}{12} = \frac{11\pi}{6} + \frac{\pi}{4}$$

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$$\frac{25\pi}{12} = \frac{11\pi}{6} + \frac{\pi}{4}$$
 54. $\frac{19\pi}{12} = \frac{11\pi}{6} - \frac{\pi}{4}$

In Exercises 55-58, write the expression as the sine, cosine, or tangent of an angle.

55.
$$\sin 60^{\circ} \cos 45^{\circ} - \cos 60^{\circ} \sin 45^{\circ}$$

56.
$$\cos 45^{\circ} \cos 120^{\circ} - \sin 45^{\circ} \sin 120^{\circ}$$

57.
$$\frac{\tan 25^\circ + \tan 10^\circ}{1 - \tan 25^\circ \tan 10^\circ}$$
 58. $\frac{\tan 68^\circ - \tan 115^\circ}{1 + \tan 68^\circ \tan 115^\circ}$

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In Exercises 59-64, find the exact value of the trigonometric function given that $\sin u = \frac{3}{4}$ and $\cos v = -\frac{5}{13}$ (Both uand v are in Quadrant II.)

59.
$$\sin(u + v)$$

60.
$$tan(u + v)$$

61.
$$\cos(u - v)$$

62.
$$\sin(u - v)$$

63.
$$\cos(u + v)$$

64.
$$tan(u - v)$$

In Exercises 65-70, verify the identity.

65.
$$\cos\left(x + \frac{\pi}{2}\right) = -\sin x$$
 66. $\sin\left(x - \frac{3\pi}{2}\right) = \cos x$

$$66. \sin\left(x - \frac{3\pi}{2}\right) = \cos x$$

67.
$$\cot\left(\frac{\pi}{2} - x\right) = \tan x$$
 68. $\sin(\pi - x) = \sin x$

$$68. \sin(\pi - x) = \sin x$$

69.
$$\cos 3x = 4 \cos^3 x - 3 \cos x$$

70.
$$\frac{\sin(\alpha + \beta)}{\cos \alpha \cos \beta} = \tan \alpha + \tan \beta$$

In Exercises 71-74, find all solutions of the equation in the interval $[0, 2\pi)$.

71.
$$\sin\left(x + \frac{\pi}{4}\right) - \sin\left(x - \frac{\pi}{4}\right) = 1$$

72.
$$\cos\left(x + \frac{\pi}{6}\right) - \cos\left(x - \frac{\pi}{6}\right) = 1$$

73.
$$\sin\left(x + \frac{\pi}{2}\right) - \sin\left(x - \frac{\pi}{2}\right) = \sqrt{3}$$

74.
$$\cos\left(x + \frac{3\pi}{4}\right) - \cos\left(x - \frac{3\pi}{4}\right) = 0$$

5.4 Quiz Extra Review: Chapter 5 Review p. 420 #51 – 73 odd (CHOOSE ANY 5 PROBLEMS TO COMPLETE.)

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