

Tuesday, February 19, 2019  
6:21 PM

KEY

### 5.3 D – Solving Trigonometric Equations

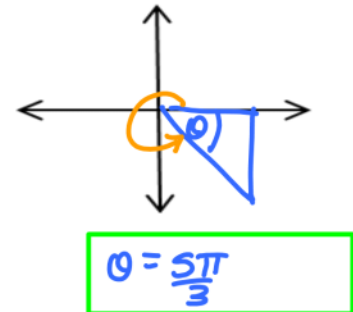
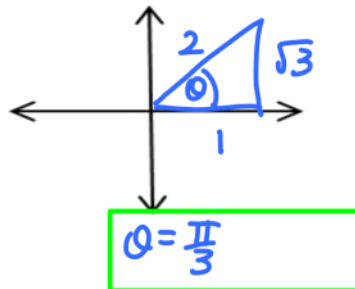
- Homework:**
- ♦ Section 5.3D
  - ♦ Quiz 5.1 – 5.3 *Monday*

**Do Now:**

Solve  $2\cos\theta - 1 = 0$  over  $[0, 2\pi)$

$$2\cos\theta = 1$$
$$\cos\theta = \frac{1}{2}$$

S	A
T	C



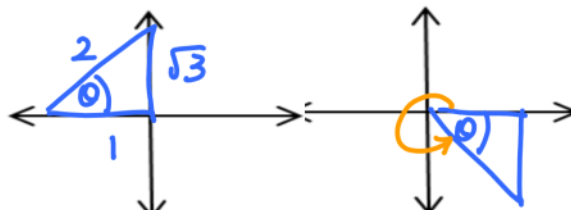
*Homework Questions??*

## Solving Multiple Angle Trig Equations

Solve:  $2 \cos 2\theta - 1 = 0$

$2 \cos 2\theta = 1$

$\cos 2\theta = \frac{1}{2}$



$\frac{1}{2}(2\theta) = \left(\frac{\pi}{3} + 2\pi n\right) \frac{1}{2}$

$\theta = \frac{\pi}{6} + \pi n$

$\frac{1}{2}(2\theta) = \left(\frac{5\pi}{3} + 2\pi n\right) \frac{1}{2}$


$\theta = \frac{5\pi}{6} + \pi n$

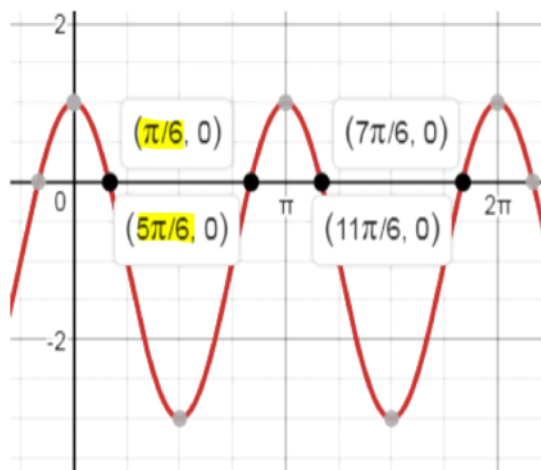
- ① Solve the equation for “ $2\theta$ ”.
- ② Set the angle values found equal to “ $2\theta$ ” and solve for “ $\theta$ ”

What is the period of this function?  $\frac{2\pi}{6} = \frac{2\pi}{2} = \pi$

How does that connect to your solution?  $\neq$  ADD  $\pi$  (or  $\frac{6\pi}{6}$ ) TO GET OTHER SOLUTIONS

We can check our solutions by graphing!

  $2 \cos(2x) - 1$



Find all solutions in the interval  $[0, 2\pi)$ :

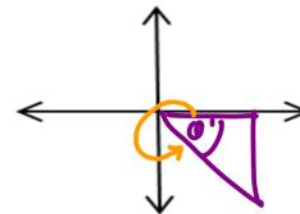
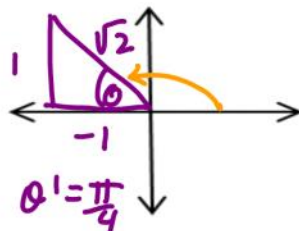


$$3 \tan 3x + 3 = 0$$

$$\frac{S}{T} = \frac{A}{C}$$

$$\frac{3 \tan 3x}{3} = \frac{-3}{3}$$

$$\tan 3x = -1$$



$$\frac{1}{3}(3\theta) = \left(\frac{3\pi}{4} + \pi n\right) \frac{1}{3}$$

$$\frac{1}{3}(3\theta) = \left(\frac{7\pi}{4} + \pi n\right) \frac{1}{3}$$

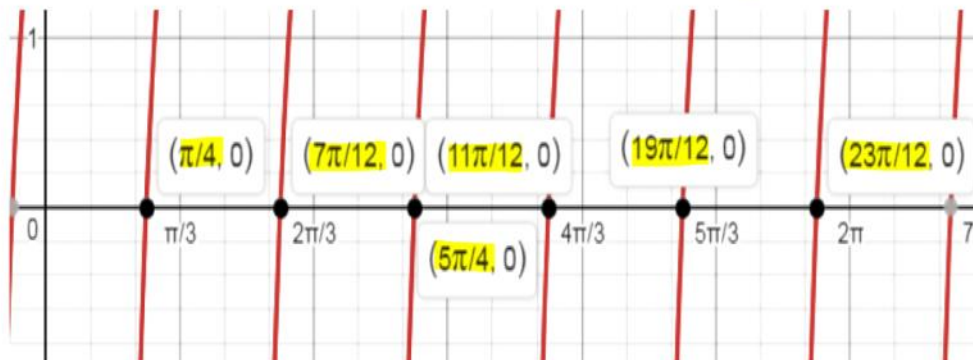
$$\frac{3\pi}{12} = \theta = \frac{\pi}{4} + \frac{\pi n}{3}$$

$$\theta = \frac{7\pi}{12} + \frac{\pi n}{3}$$

What is the period of this function?

$$T = \frac{\pi}{3} \cdot \frac{4}{1}$$

\*ADD  $\frac{4\pi}{12}$  to get other solutions



$$\left(\frac{11\pi}{12}, \frac{15\pi}{12}\right)$$

$$\left(\frac{19\pi}{12}, \frac{23\pi}{12}\right)$$

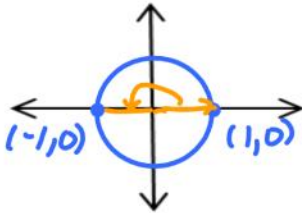
Find all solutions in the interval  $[0, 2\pi)$ :



$$\sin^2 2x + \sin 2x = 0$$

$$\sin 2x (\sin 2x + 1) = 0$$

$$\sin 2x = 0$$



$$\frac{1}{2}(2x) = (0 + 2\pi n) \pm$$

$$x = 0 + \pi n$$

$$x = 0, \pi$$

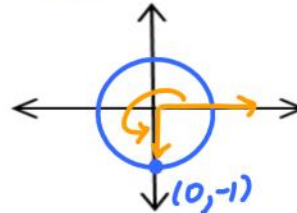
$$\frac{1}{2}(2x) = (\pi + 2\pi n) \pm$$

$$x = \frac{\pi}{2} + \pi n$$

$$x = \frac{\pi}{2}, \frac{3\pi}{2}$$

$$\sin 2x + 1 = 0$$

$$\sin 2x = -1$$



$$\frac{1}{2}(2x) = \left(\frac{3\pi}{2} + 2\pi n\right) \pm$$

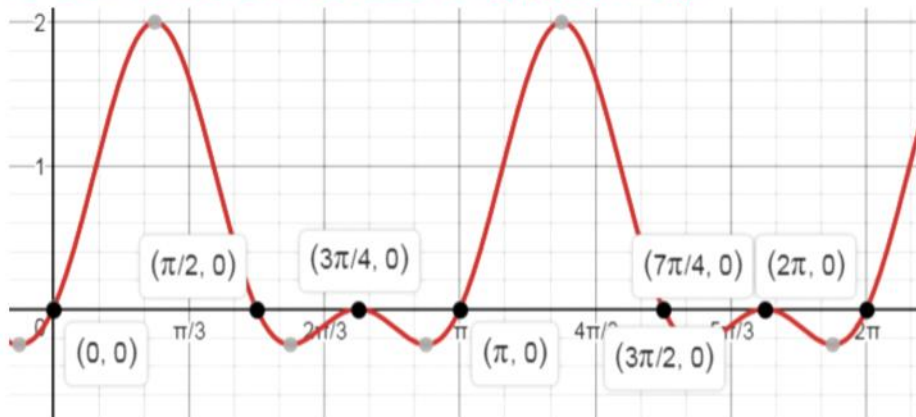
$$x = \frac{3\pi}{4} + \pi n$$

$$x = \frac{3\pi}{4}, \frac{7\pi}{4}$$

What is the period of this function?  $\frac{2\pi}{b} = \frac{2\pi}{2} = \pi$

\* TO GET ALL SOLUTIONS  
ADD MULTIPLES  
OF  $\pi$ .

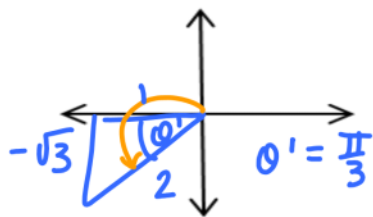
We can check our solutions by graphing!



Solve the equation:

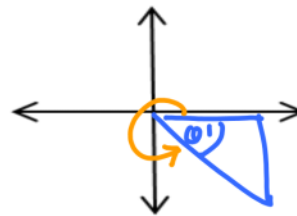
$$\sin\left(\frac{x}{2}\right) = -\frac{\sqrt{3}}{2}$$

$$\frac{S}{T/C}$$



$$2\left(\frac{1}{2}x\right) = \left(\frac{4\pi}{3} + 2\pi n\right) 2$$

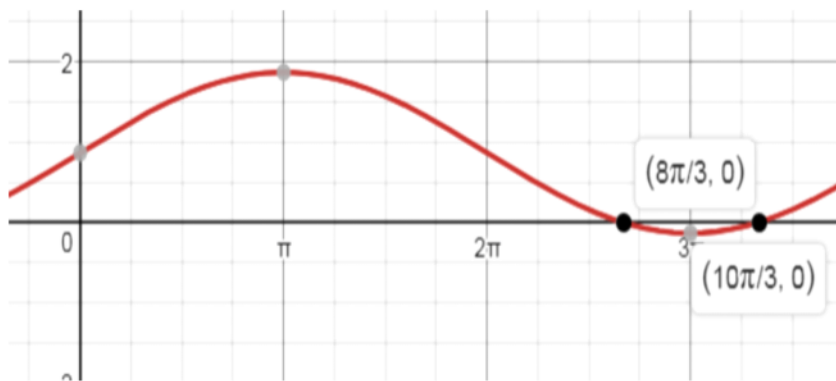
$$x = \frac{8\pi}{3} + 4\pi n$$



$$2\left(\frac{1}{2}x\right) = \left(\frac{5\pi}{3} + 2\pi n\right) 2$$

$$x = \frac{10\pi}{3} + 4\pi n$$

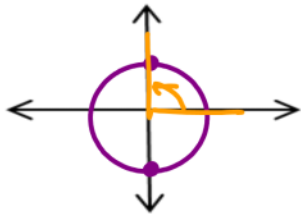
What is the period of this function?  $\frac{2\pi}{b} = \frac{2\pi}{\frac{1}{2}} = 4\pi$



Solve the equation:

$$\cos 2y (\cos y - 1) = 0$$

$$\cos 2y = 0$$



$$\frac{1}{2}(2y) = \left(\frac{\pi}{2} + 2\pi n\right) \frac{1}{2}$$

$$y = \frac{\pi}{4} + \pi n$$

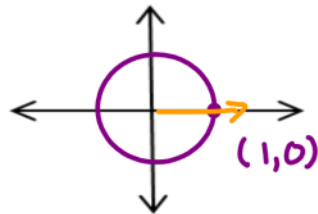
$$\frac{1}{2}(2y) = \left(\frac{3\pi}{2} + 2\pi n\right) \frac{1}{2}$$

$$y = \frac{3\pi}{4} + \pi n$$

$$* \text{period} = \frac{2\pi}{6} = \frac{2\pi}{2} = \pi$$

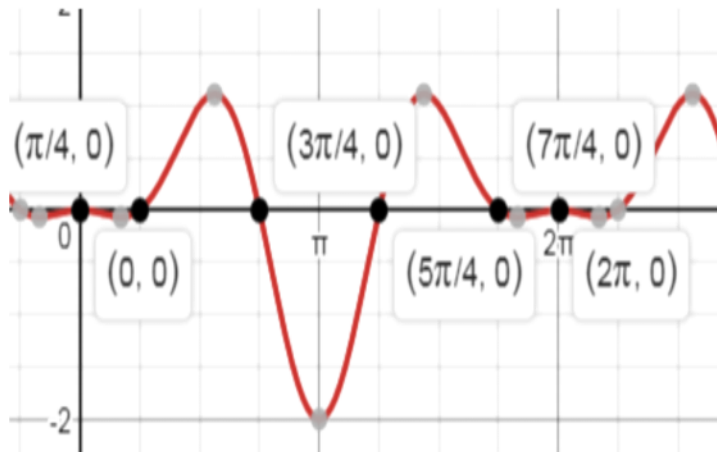
$$\cos y - 1 = 0$$

$$\cos y = 1$$



$$y = 0 + 2\pi n$$

$$* \text{period} = \frac{2\pi}{6} = 2\pi$$



Find all solutions in the interval  $[0, 2\pi)$ :



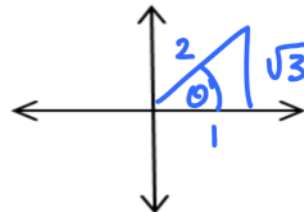
$$2 \tan^2\left(\frac{x}{2}\right) - 4 = 2$$

$$2 \tan^2\left(\frac{x}{2}\right) = 6$$

$$\sqrt{\tan^2\left(\frac{x}{2}\right)} = \sqrt{3}$$

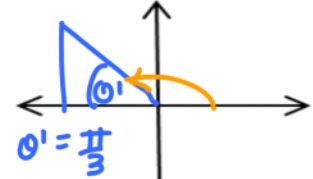
$$|\tan\left(\frac{x}{2}\right)| = \sqrt{3}$$

$$\frac{0}{a} \quad \tan\left(\frac{x}{2}\right) = \pm \sqrt{3}$$



$$2\left(\frac{1}{2}x\right) = \left(\frac{\pi}{3}\right)^2$$

$$x = \frac{2\pi}{3}$$

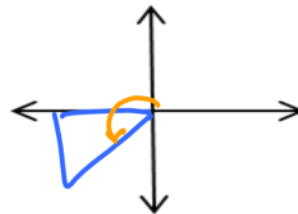


$$2\left(\frac{1}{2}x\right) = \left(\frac{2\pi}{3}\right)^2$$

$$x = \frac{4\pi}{3}$$

$$* \text{ period} = \frac{\pi}{b} = \frac{\pi}{\frac{1}{2}} = 2\pi$$

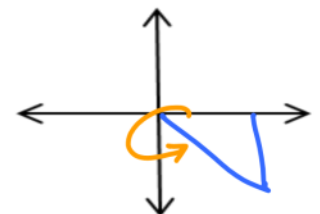
$$2\pi \cdot \frac{3}{3} = \frac{6\pi}{3}$$



$$2\left(\frac{1}{2}x\right) = \left(\frac{4\pi}{3}\right)^2$$

$$x = \frac{8\pi}{3}$$

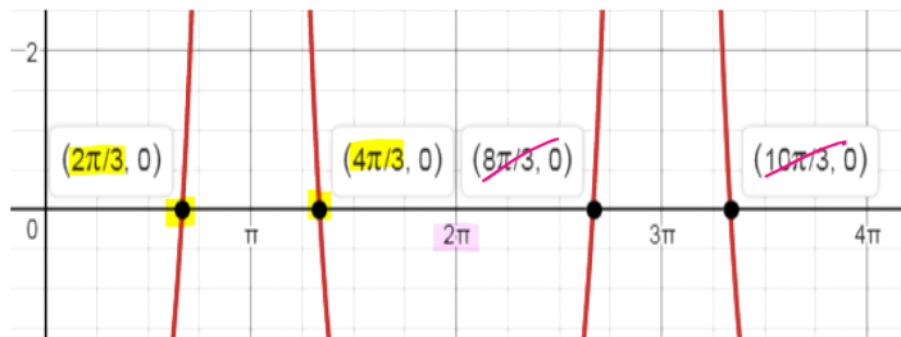
\* beyond  $2\pi$



$$2\left(\frac{1}{2}x\right) = \left(\frac{5\pi}{3}\right)^2$$

$$x = \frac{10\pi}{3}$$

\* beyond  $2\pi$





## Closure....

Using the graphing calculator.....

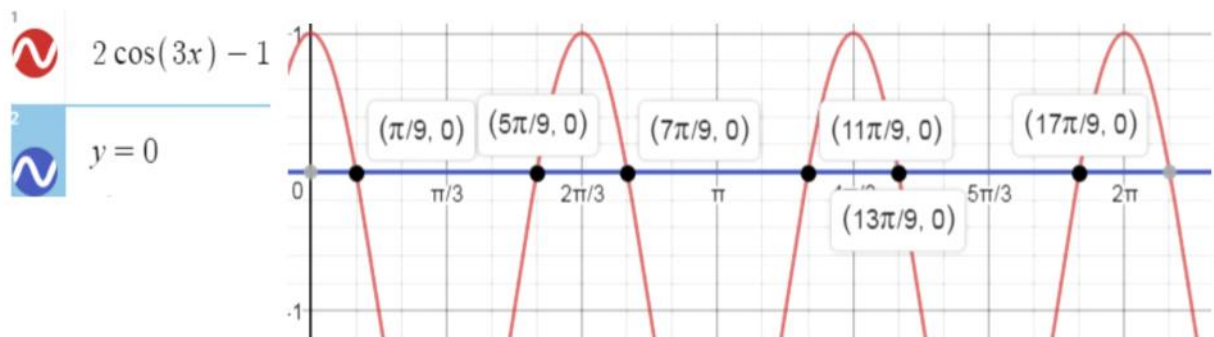
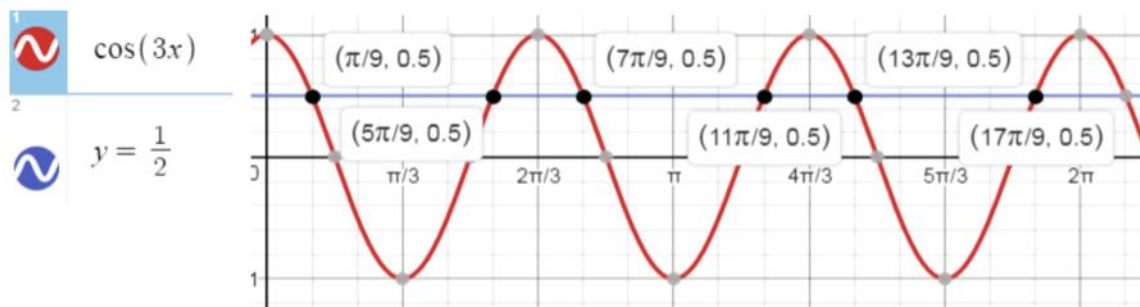
$$2 \cos 3\theta - 1 = 0$$

$$2 \cos 3\theta = 1$$

$$\cos 3\theta = \frac{1}{2}$$

What would the intersection of  $y = \cos 3\theta$  and  $y = \frac{1}{2}$  represent?

What would the intersection of  $y = 2 \cos 3\theta - 1$  and  $y = 0$  represent?



They both represent all of the solutions to original equation.