

Monday, January 14, 2019
4:52 PM

Precalc **KEY**

4.8A Applications & Models

Obj: To solve real life problems involving right triangles

Hwk: 4.8A #1, 5, 9, 11, 19, 21, 23, 25

DIF. THAN ASSIGNMENT SHEET

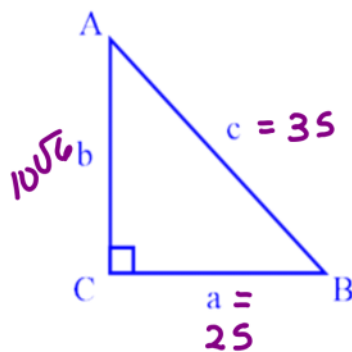
Finish 4.8 Bearings Worksheet

Do Now: Solve the right triangle when $a = 25, c = 35$.

Round to the nearest tenth.

$$\sin \theta = \frac{25}{35}$$

* Use Degree mode!



$$a^2 + b^2 = c^2$$

$$25^2 + b^2 = 35^2$$

$$625 + b^2 = 1225$$

$$b^2 = 600$$

$$b = 10\sqrt{6}$$

$$= 24.5$$

$$\sin^{-1} \frac{25}{35} = A$$

$$A = 45.6^\circ$$

$$\cos^{-1} \frac{25}{35} = B$$

$$B = 44.4^\circ$$

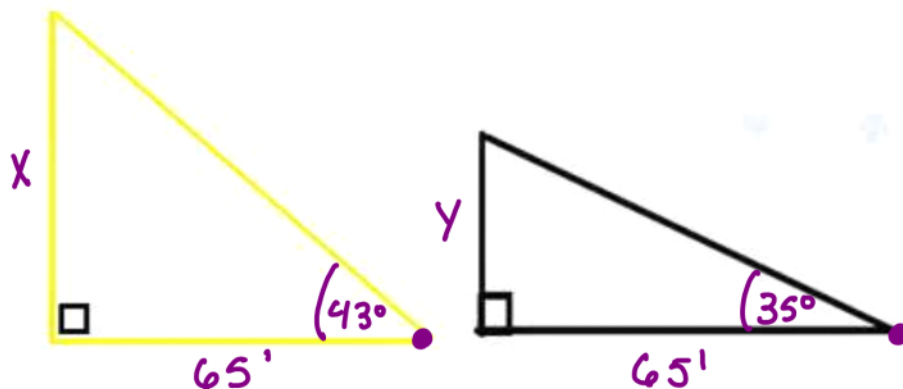
Recap:

- Angles/vertices: named with **CAPITAL LETTERS**
- Sides: named with **LOWER CASE LETTERS** OPPOSITE corresponding \angle s
- In right triangle, measure of $\angle C$ is always 90°
- To **SOLVE A RIGHT TRIANGLE**, find ALL missing sides & angles (using trig & complementary angles)

Homework Questions??

Applications Involving Right Triangles

1. From a point 65 feet in front of a church, the angles of elevation to the base of the steeple and the top of the steeple are 35° and 43° respectively. Find the height of the steeple.



$$\tan 43^\circ = \frac{X}{65}$$

$$65 \tan 43^\circ = X$$

$$X = 60.6'$$

$$\tan 35^\circ = \frac{X}{65}$$

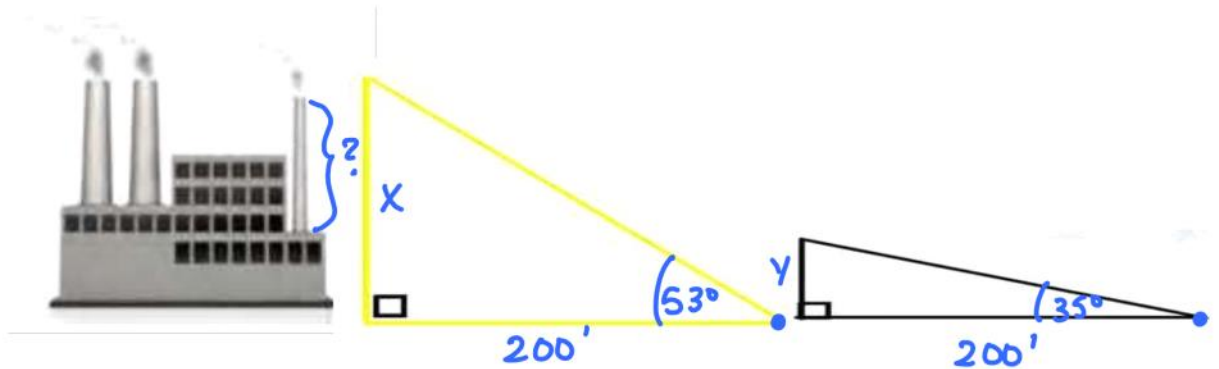
$$65 \tan 35^\circ = X$$

$$X = 45.5'$$

$$\begin{aligned} \text{Height of steeple} &= 60.6 - 45.5' \\ &= \boxed{15.1'} \end{aligned}$$

Applications Involving Right Triangles

2. At a point 200 ft. from the base of a building, the angle of elevation to the bottom of a smokestack is 35° , whereas the angle of elevation to the top is 53° . Find the height s of the smokestack.



$$\tan 53^\circ = \frac{x}{200'}$$

$$200' \tan 53^\circ = x$$

$$x = 265.4'$$

$$\tan 35^\circ = \frac{y}{200}$$

$$200 \tan 35^\circ = y$$

$$y = 140.0'$$

$$\begin{aligned} \text{Height of smokestack} &= 265.4' - 140.0' \\ &= \boxed{125.4'} \end{aligned}$$

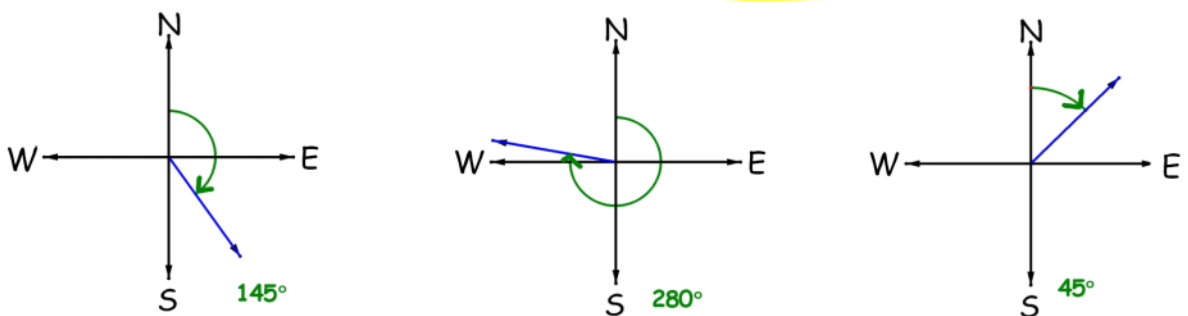
Bearing Angles (Bearings)

* In notebooks

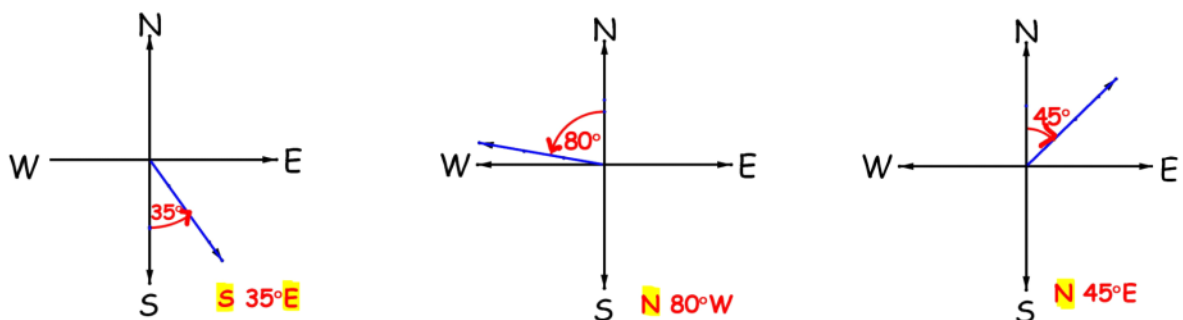
In surveying and navigation, directions are given in terms of **bearings**. A bearing measures the angle that a path or line of sight makes with a **fixed north-south line**.

There are 2 ways to express a bearing:

Airplane Bearings - When a single angle is given, the bearing is measured in a **clockwise direction from due north**.



Ship Bearings - start with a **north or south line** and uses an acute angle to indicate **rotation towards the east or west**.



Let's Practice! (on $\frac{1}{2}$ sheet)

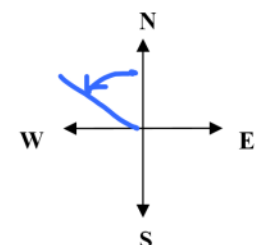
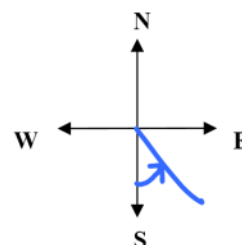
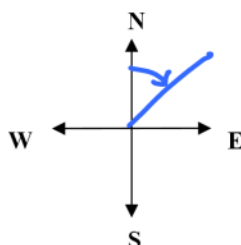
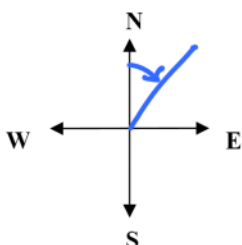
Draw a diagram that represents each bearing.

1. Bearing of 32°

2. $N 42^\circ E$

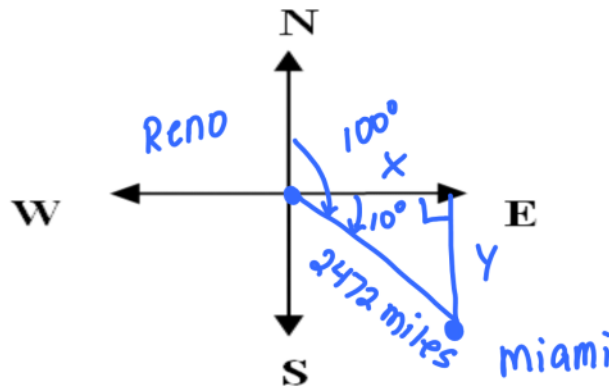
3. $S 31^\circ E$

4. $N 52^\circ W$



Applications Involving Bearings (back of $\frac{1}{2}$ sheet)

- 1.) A jet leaves Reno, Nevada and is headed toward Miami, Florida at a bearing of 100° . The distance between the two cities is approximately 2472 miles. How far north and how far west is Reno relative to Miami?



$$\sin 10^\circ = \frac{y}{2472 \text{ miles}}$$

$$2472 \sin 10^\circ = y$$

$$y = 429.3 \text{ miles north}$$

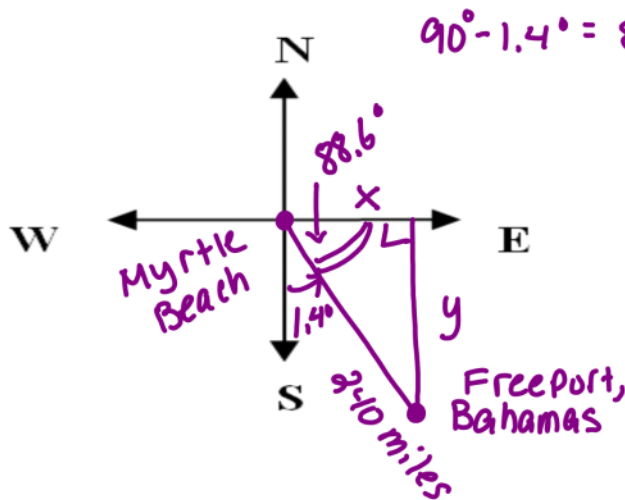
$$\cos 10^\circ = \frac{x}{2472}$$

$$2472 \cos 10^\circ = x$$

$$x = 2434.4 \text{ miles west}$$

- 2.) A yacht leaves a dock in Myrtle Beach, SC & heads toward Freeport, Bahamas at a bearing of $S 1.4^\circ E$. If the ship travels as a speed of 20 knots (nautical miles per hour), how far east and south is the yacht after 12 hours?

$$20 \times 12 = 240 \text{ miles}$$



$$\sin 88.6^\circ = \frac{y}{240}$$

$$240 \sin 88.6^\circ = y$$

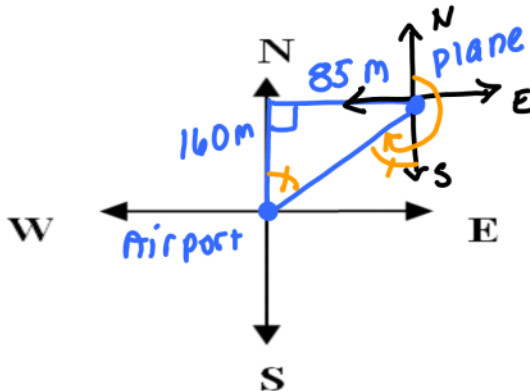
$$y = 239.9 \text{ miles south}$$

$$\cos 88.6^\circ = \frac{x}{240}$$

$$240 \cos 88.6^\circ = x$$

$$x = 5.9 \text{ miles east}$$

- 3.) An airplane is 160 miles north and 85 miles east of an airport. The pilot wants to fly directly to the airport. What bearing should be taken?



$$\tan \theta = \frac{85}{160}$$

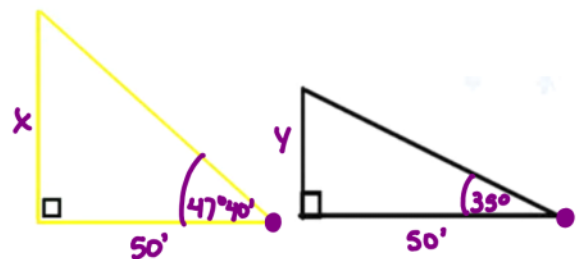
$$\tan^{-1} \frac{85}{160} = 28^\circ$$

$$180^\circ + 28^\circ = 208^\circ$$

Closure:

A Quick Look at HW.....

- 19.) **Height** - From a point 50 feet in front of a church, the angles of elevation to the base of the steeple and the top of the steeple are 35° and $47^\circ 40'$ respectively.
- Draw right triangles that give a visual representation of the problem. Label the known and unknown quantities.
 - Use a trigonometric function to write an equation involving the unknown quantity.
 - Find the height of the steeple.



- 25.) A cellular telephone tower that is 150 feet tall is placed on top of a mountain that is 1200 feet above sea level. What is the angle of depression from the top of the tower to a cell phone user who is 5 horizontal miles away and 400 feet above sea level?

