

Wednesday, October 18, 2017
6:21 PM

Precalculus
1.6 – 1.8 Review

Name: KEY
Period: _____ Date: _____

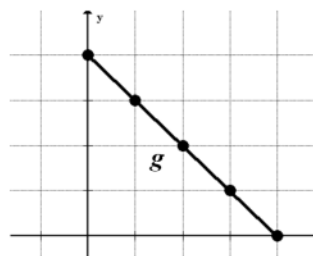
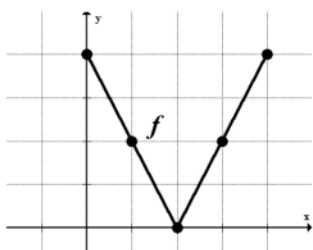
In Exercises 1–2, find a) $(f+g)(x)$, b) $(f-g)(x)$, c) $(fg)(x)$, d) $(f/g)(x)$. What is the domain of f/g ?

| | | | |
|---|---|---|--|
| 1. $f(x) = 2x - 5$ and $g(x) = 2 - x$ | | 2. $f(x) = x^2 - 1$ and $g(x) = \sqrt{3-x}$ | |
| 1a) $2x-5 + 2-x$ $= x-3$ | 1b) $2x-5 - (2-x) =$ $3x-7$ | 2a) $x^2-1 + \sqrt{3-x}$ | 2b) $x^2-1 - \sqrt{3-x}$ |
| 1c) $(2x-5)(2-x) =$ $4x - 2x^2 - 10 + 5x$ $= -2x^2 + 9x - 10$ | 1d) $\frac{2x-5}{2-x}$ $x-2 \neq 0$ $x \neq 2$ D: $(-\infty, 2) \cup (2, \infty)$ | 2c) $(x^2-1)(\sqrt{3-x})$ | 2d) $\frac{x^2-1}{\sqrt{3-x}}$ $3-x > 0$ $-x > -3$ $x < 3$ $(-\infty, 3)$ |

In Exercises 3–4, find a) $f \circ g$, b) $g \circ f$, c) $f \circ f$, d) $g \circ g$.

| | |
|---|--|
| 3. $f(x) = x^2 + 2$ and $g(x) = 3 - x$ | |
| 3a) $f(g(x)) = (3-x)^2 + 2 = (3-x)(3-x) + 2$ $= 9 - 6x + x^2 + 2$ $= x^2 - 6x + 11$ | 3b) $g(f(x)) = 3 - (x^2 + 2)$ $= 3 - x^2 - 2$ $= -x^2 + 1$ |
| 3c) $f(f(x)) = (x^2 + 2)^2 + 2$ $= (x^2 + 2)(x^2 + 2) + 2$ $= x^4 + 4x^2 + 4 + 2$ $= x^4 + 4x^2 + 6$ | 3d) $g(g(x)) = 3 - (3 - x)$ $= 3 - 3 + x$ $= x$ |

In Exercises 4–11, use the graphs of f and g to evaluate the functions.



| | | | |
|--|---|--|--|
| 4) $(f+g)(1)$ $f(1) + g(1) =$ $2 + 3 =$ 5 | 5) $(fg)(3)$ $f(3) \cdot g(3) =$ $2 \cdot 1 =$ 2 | 6) $(f \circ g)(2)$ $g(2) = 2$ $f(2) = 0$ | 7) $(g \circ f)(4)$ $f(4) = 4$ $g(4) = 0$ |
| 8) $(g-f)(0)$ $g(0) - f(0) =$ $4 - 4 =$ 0 | 9) $\left(\frac{g}{f}\right)(4)$ $\frac{g(4)}{f(4)} = \frac{0}{4} = 0$ | 10) $(f \circ f)(2)$ $f(2) = 0$ $f(0) = 4$ | 11) $(g \circ g)(3)$ $g(3) = 1$ $g(1) = 3$ |

In Exercises 12 – 13, write an equation for the function that has

12) the parent graph $f(x) = \llbracket x \rrbracket$
 stretched twice vertically
 reflected in the y-axis
 shifted 3 units to the right and 1 units upward

$$h(x) = 2 \llbracket -(x-3) \rrbracket + 1$$

13) the parent graph $f(x) = |x|$
 shrunk horizontally with coefficient 3
 reflected in the x-axis
 shifted 2 units to the left and 1 units downward

$$k(x) = -|/3(x+2)| - 1$$

In Exercises 14 – 15, identify the parent function and describe the sequence of transformations. Sketch the graph for each of the transformed functions. **DO NOT USE A CALCULATOR!!!**

14). $f(x) = -(-x+1)^2$ $p(x) = x^2$

| x | y | $(-1)x$ | $x+1$ | $(-1)y$ |
|-----|-----|---------|-------|---------|
| 2 | 4 | 2 | 3 | -4 |
| 1 | 1 | 1 | 2 | -1 |
| 0 | 0 | 0 | 1 | 0 |
| -1 | 1 | -1 | 0 | -1 |
| -2 | 4 | -2 | -1 | -4 |

*** FACTOR OUT negative!**

- Reflect over y-axis
- Shift 1 RT
- Reflect over x-axis

15). $f(x) = 3\sqrt{1-x} - 4$ $p(x) = \sqrt{x}$

| x | y | $x(-1)$ | $x+1$ | $3(y)$ |
|-----|-----|---------|-------|--------|
| 0 | 0 | 0 | 1 | 0 |
| 1 | 1 | 1 | 2 | 3 |
| 4 | 2 | 4 | 5 | 6 |
| 9 | 3 | 9 | 10 | 9 |

*** FACTOR OUT negative!**

- Reflect over y-axis
- Shift 1 RT
- Vertical stretch by 3
- Shift 4 down

In Exercises 16–17, use the graph of f below to sketch the graph of g (on the same set of axes). List your ordered pairs for each!

16). $g(x) = f\left(\frac{1}{2}x\right) - 1$

| x | y | $2(x)$ | $y-1$ |
|-----|-----|--------|-------|
| -4 | 5 | -8 | 4 |
| -2 | 1 | -4 | 0 |
| 0 | 0 | 0 | -1 |
| 1 | 3 | 2 | 2 |
| 4 | -3 | 8 | -4 |

*** Reciprocal**

*** HORIZONTAL stretch by 2**
*** Shift 1 down**

17). $g(x) = 2f(-x)$

| x | y | $(-1)x$ | $2(y)$ |
|-----|-----|---------|--------|
| -4 | 5 | 4 | 10 |
| -2 | 1 | 2 | 2 |
| 0 | 0 | 0 | 0 |
| 1 | 3 | -1 | 6 |
| 4 | -3 | -4 | -6 |

*** Reflect over y-axis**
*** Vertical stretch by 2**